



## Einladung

zum

## Oberseminar Stochastik

am Mittwoch, dem **14. Februar 2018**, um **17 Uhr** im **Seminarraum 2**  
des Mathematischen Instituts (Raum 204), Weyertal 86–90, 50931 Köln

Es spricht

**Siva Athreya**  
(Indian Statistical Institute Bangalore, India)

zum Thema

### Small noise limit for singularly perturbed diffusions.

We consider a simultaneous small noise limit for a singularly perturbed coupled diffusion described by

$$\begin{aligned}X_t^\varepsilon &= x_0 + \int_0^t b(X_s^\varepsilon, Y_s^\varepsilon) ds + \varepsilon^\alpha B_t, \\Y_t^\varepsilon &= y_0 - \frac{1}{\varepsilon} \int_0^t \nabla_y U(X_s^\varepsilon, Y_s^\varepsilon) ds + \frac{s(\varepsilon)}{\sqrt{\varepsilon}} W_t,\end{aligned}$$

where  $x_0 \in \mathbb{R}^d, y_0 \in \mathbb{R}^m, B_t, W_t$  are independent Brownian motions,

$b: \mathbb{R}^d \times \mathbb{R}^m \rightarrow \mathbb{R}^d, U: \mathbb{R}^d \times \mathbb{R}^m \rightarrow \mathbb{R}$ , and  $s: (0, \infty) \rightarrow (0, \infty)$ .

One observes that there is a time scale separation between  $X$  and  $Y$ . Under suitable assumptions on  $b, U$ , for  $0 < \alpha < \frac{1}{2}$ , if  $s(\varepsilon) \rightarrow 0$  goes to zero at a prescribed slow enough rate then we establish all weak limits points of  $X^\varepsilon$ , as  $\varepsilon \rightarrow 0$ , as Fillipov solutions to a differential inclusion.

This is joint work with V. Borkar, S. Kumar and R. Sundaresan.

Alle Interessenten sind herzlich eingeladen.

Die Dozenten der Stochastik